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The Relation between the Teaching of Mathematics and the Teaching of Statistics in the South African Context

Lukanda Kalobo

Athens Institute for Education and Research 8 Valaoritou Street, Kolonaki, 10683 Athens, Greece

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Lukanda Kalobo, Lecturer, Central University of Technology, Free State, South Africa

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ABSTRACT

The study of Statistics can be fully integrated into the Mathematics Curriculum, giving it meaning to everyday life. Statistical activities in the classroom can be directly linked to the learners' personal interests and stimulate their motivation for numerical and quantitative studies. Hence, it is important to develop children's mental images of numbers parallel to their acquisition of counting and calculation skills; skills that Mathematics and Statistics present. The purpose of this study is to explore the relation between the teaching of Mathematics and the teaching of Statistics at high school level in the South African Context. Furthermore, the study examines and analyses examples of statistical teaching situations from both a mathematical and a statistical perspective with view to reveal the links between the teaching of Mathematics and teaching of Statistics. A non-empirical method or conceptual method was followed to achieve the purposes of the study. To this end, a literature review characterised by document analysis was used to answer to the critical aspects of the study. The study reveals the cardinal links between the teaching of Mathematics and teaching of Statistics. Hence the call to educators to acknowledge the symbiosis to enhance the teaching and promote an awareness of the ways in which Statistics is presented and aligned in the South African Mathematics high school Curriculum.

Keywords: teaching mathematics, teaching statistics, high school, South African context

Introduction

It is not astonishing that in South Africa, Statistics instruction at High school is compulsory for all learners taking Mathematics. Statistics is a part of the Mathematics curricula in basic education (Department of Basic Education [DBE], 2005). According to Burril (2011), the goal of teaching Statistics is to foster an adult population capable of reasoning from, and about data and making informed decisions based on quantitative information in the workplace, in their personal lives and as citizens. Furthermore, Citizens are being called upon to make increasingly complex decisions about policies and practices in the socio-political, workplace, and consumer arenas (Franklin & Garfield, 2006; Kader & Perry, 2006). Thus, the teaching of Statistics provides learners with tools and ideas to use in order to react intelligently to quantitative information in their world (Ben-Zvi & Garfield, 2008). At the other end Mathematics helps to develop mental processes that enhance logical and critical thinking, accuracy and problem solving that will contribute in decision -making (DBE, 2011). According to DBE (2011) Mathematics problem solving enables us to understand the world (physical, social, and economical) around us, and, most of all, to teach us to think creativity. The goal of mathematical instruction should be to make students sensible, critical users of Statistics, able to apply their processes and principles to real-world problems (Mathematics Curriculum Framework, 1996). This is manifest in the South African Mathematics Curriculum and Assessment Policy Statement (CAPS), with one of the aims is to collect, analyse, organise, and critically evaluate information (DBE, 2011). This study emphasis on the need to explore the relation between the teaching of Mathematics and the teaching of Statistics at high school level in the South African Context.

Literature Review

The literature focuses on the teaching of Mathematics and teaching of Statistics. A considerable number of sources on didactics are available in both theory and practice. There is, however, a paucity of literature in South Africa relating to the teaching of Statistics at high schools; the researcher relied on available overseas literature on these topics and the South African Mathematics Curriculum.

Conceptualisation of the Teaching of Mathematics in the South African Context

Given that there are different competing influences in Mathematics, it is important to clarify to the reader how teaching of Mathematics has been conceptualised in this paper. Pimm, Westwell, Wilder and Wilder (2011) spoke about four Mathematics perspectives such as the industrial pragmatists, the mathematical purists, the progressive educators, and the social reformers. This study presents extracts that include brief descriptions of Mathematics perspectives, published in Mathematics education literature, from the progressive educators,

and the social reformers. Conferring to Pimm et al. (2010), the progressive educators are concerned with the personal development of pupils, with the individual child as the focus of attention (Pimm et al., 2010). Additionally, Berry III and Ellis (2005) agreed that the progressive educators assert that children should have the freedom to develop naturally; interest should be the motivation for all work, and the teacher is a guide and not a taskmaster. Pimm et al. (2011) revealed that the teacher's role is perceived by the progressive educators as guiding the learners on their journeys of discovery contexts. Pimm et al. (2011) explained that the social reformers are concerned with the social development of pupils, in the sense that education should empower the individual to participate fully and critically in a democratic society. Furthermore, Ernest (1991, p. 207) confirmed that this group views Mathematics as a social construction: tentative, growing by means of human creation and decisionmaking, and connected with other realms of knowledge, culture, and social life. Additionally, for Pimm et al. (2011) the social reformers perceive the teacher's role as facilitating learners in both posing and solving their own problem contexts. Moreover, any form of assessment must be seen to be fair to all pupils and should not disadvantage any social group. This require a greater variety of modes of assessment and so project work and the ongoing assessment of coursework is highly valued (Pimm et al., 2011).

Thus, the South African views of Mathematics are closely associated with those of the progressive educators and the social reformers. The South African Curriculum has recently been restructured to reflect the values and principles of a democratic society. In view of the country's history and legacy of inequality, curricula have been developed to accommodate the widely different groups (Steffens & Fletcher, 1999). In South Africa, the Mathematics Curriculum is concerned about the personal development of learners. This Curriculum supports a learner-centred teaching approach whereby the teacher is the one that exposes learners to mathematical experiences that give them many opportunities to develop their mathematical reasoning and creative skills in preparation for more abstract Mathematics in Higher/Tertiary Education institutions (DBE, 2011). Furthermore, the Curriculum promotes the participation of learners as responsible citizens in the life of local, national, and global communities; use mathematical process skills to identify, investigate and solve problems creatively and critically (DBE, 2011). Moreover, according to DBE (2011), the Mathematics Curriculum views assessment as a continuous planned process of identifying, gathering and interpreting information about the performance of learners, using various forms of assessment. The teachers' conception of Mathematics significantly influences how they teach it. Furthermore, these DBE's views have been supported by Beckmann, Thompson, and Rubenstein (2009), acknowledging that teaching Mathematics means supporting learners as they learn to think more and more about Mathematics notions, processes, applications, and relationships.

Conceptualisation of the Teaching of Statistics in the South African Context

Doing Statistics involves many primarily nonmathematical activities, such as building meaning for data by examining the context and choosing appropriate study designs to answer questions of interest (Randall & Growth, 2007). According to Burril (2011), the aim of teaching Statistics is to foster an adult population capable of reasoning from, and about data and making informed decisions based on quantitative information in the workplace, in their personal lives and as citizens. The teaching of Statistics provides learners with tools and ideas to use in order to react intelligently to quantitative information in their world. Burril (1996) revealed that in teaching Statistics attention must also be paid to the didactics of the Statistics classroom, and statistical concepts should be learned over time beginning with early and informal experiences. According to delMas (2002), using statistical literacy, reasoning, and thinking to distinguish between desired learning outcomes in Statistics is extremely helpful both in considering instructional goals and in writing assessment items. Statistical literacy includes basic and important skills that may be used in understanding statistical information or research results (Chance, delMas & Garfield, 2003). One of the ways that seems especially favoured to help students develop their statistical reasoning is to incorporate active-learning strategies where students are allowed to practice statistics by designing a study, collecting data, analysing the results and preparing reports, even giving oral presentations. This aids in building students' sense of responsibility for learning and turns them into active constructors of their education (Cobb, 1993). Statistical thinking is promoted when instruction challenges learners to apply their understanding to real-world problems, to critique and evaluate the design and conclusions of studies, or to generalise knowledge obtained from classroom examples to new and somewhat novel situations (Chance, 2002).

Statistical Teaching Situations from Both a Mathematical and a Statistical Perspective

Constructivism Approach

Constructivism is an approach to learning that holds that people actively construct or make their own knowledge and that reality is determined by the experiences of the learner' (Elliott et al., 2000). This constructivist view implies that learners work actively towards constructing their own knowledge and combining it with the knowledge they already have (Moore, 1997). One of the general aims of the South African Curriculum is to encourage an active and critical approach to learning, rather than rote and uncritical learning of given truths (DBE, 2011). Constructivism's central idea is that human learning is constructed, that learners build new knowledge upon the foundation of previous learning. This educational view changes not only the learners' but also the teachers' perspective in Mathematics. Moore (1997) proposes a shift from a theoretical approach to a more direct way of learning in Mathematics. Based on the relevant research in the context of constructivist principles, Garfield (1995) formulated general principles

of learning Statistics based on constructivism practice. Constructivist practice is thus applied in both teaching Mathematics and teaching Statistics. In the South African context, there is a need for the teacher to acknowledge that constructivist practice plays an important role in the teaching of Mathematics and in the teaching of Statistics in the Mathematics Curriculum.

Existing Knowledge

The focus of teaching and learning Statistics at high school is built on what was learned previously in lower grades (DBE, 2003). Therefore, learners come to high school with the existing knowledge of Mathematics or Statistics from previous Grades. Gattuso (2006) confirms that it is essential to highlight the mathematical concepts underlying the statistical concepts, in order to link both in creating classroom activities. If learners' initial ideas and beliefs are ignored, the understandings that they develop can differ a great deal from the teacher's intentions.

For example, learners are asked to represent the data of COVID-19 death cases in South Africa in a box plot format (see Table 1). The box plot (see Figure 1) is used to examine data. This format is often referred to as a box-and-whisker plot. Box plots are useful for comparing different sets of data (Triola, 2011: 122).

Table 1. COVID-19 Pandemic in South Africa

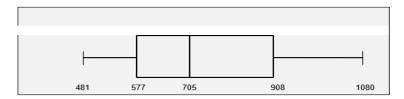
Date	Deaths
2020-05-25	481
2020-05-26	524
2020-05-27	552
2020-05-28	577
2020-05-29	611
2020-05-30	643
2020-05-31	683
2020-06-01	705
2020-06-02	755
2020-06-03	792
2020-06-04	848
2020-06-05	908
2020-06-06	952
2020-06-07	998
2020-06-08	1080

The learners should conclude that the minimum is 481 and the maximum is 1080. The first quartile involves the concept of percentage. In this instance, learners need to find the 25th percentile of a given data.

Let h be the total. Let k be the percentile being used, L the position of value, P_k the k^{th} percentile. So $L = k \times h$, $k = \frac{25}{100}$, h = 15 this implies that $L = \frac{25}{100} \times 15 = 3.75$. Thus $Q_1 = 577$. The second quartile involves 50^{th}

percentile. Learners must remember how to calculate 50% of a given amount. This implies that $L = \frac{50}{100} \times 15 = 7.5$. Thus $Q_2 = 705$. Similarly, $Q_3 = 908$.

Figure 1. The Box-and-Whisker Plot Representing the Population Age



Therefore, the statistical concept of the five number summary can be introduced. The box plot representing the data can be drawn and this five number summary can be interpreted. The link between the teaching of Mathematics and the teaching of Statistics is evident in the prior mathematical knowledge needed by the learners in Statistics to find the minimum (min = 481) and maximum (max = 1080); the calculations of 25% (Q1 = 577), the 50% (Q2 = 705) and the 75% (Q3 = 908) of a given set of data that will lead to the representation of the box plot and the interpretation of the data.

According to Gattuso (2006), it is important to let the learners explore situations in which they collect, organise and represent their own data, and make them realise the elements that are essential and those such as titles and scales that are missing. Once they display their own data in a graph or table, it is time to interpret it. This may start with counting and proceed to comparisons. This viewpoint is in line with the constructivist approach to instructional design where the teaching and learning of new concepts is based on existing knowledge.

Problem Solving

Problem solving helps a learner master a concept and that instruction should not separate Mathematics from its applications (Gattuso, 2006). According to Krulik and Posamentier (1998), the following strategies are applied to an everyday problem-solving situation in Mathematics: working backwards; finding a pattern; adopting a different point of view; solving a simple analogous problem; considering extreme cases; making a drawing; intelligent guessing and testing; accounting for all possibilities; organising data, and logical reasoning. The study of Statistics can be fully integrated into the Mathematics Curriculum, giving it meaning related to everyday life (Gattuso, 2006). Statistical activities in the classroom can be directly linked to the learners' personal interests and stimulate their motivation for numerical and quantitative studies. These activities can be used for learning, practice, assessment, and problem-solving. The following examples illustrate the use of some problem-solving strategies in Statistics such as organising data strategy and making drawing strategy.

Organising Data Strategy

For example, the last seven Easter periods (from 2014 to 2020) have seen car accident fatalities over the Easter weekend.

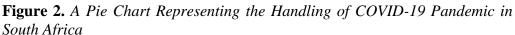
Find the median for the following group of 7 Easter periods car accident fatalities. Learners can use the organising data strategy. The way the data have been listed makes it difficult to find the median directly. However, if the data are organised in increasing/decreasing order, the middle or median is found.

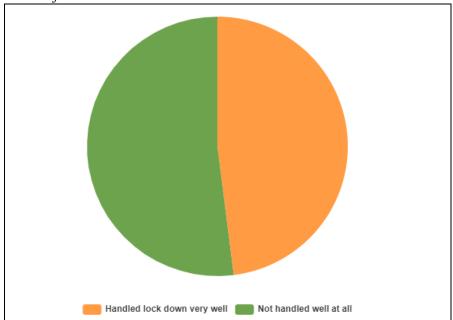
The middle or median of the data is equal to 28. In doing so, learners not only enhance their understanding of Mathematics but also get in touch with another discipline such Statistics (Gattuso, 2006).

Making Drawing Strategy

For example, views on the handling of the pandemic by the South African Government: 48% of respondents feel that the Government has handled the lockdown and pandemic crisis very well, while 52% believe it has not been handled well at all. Display and compare the given data.

The data associated with this question could be represented by means of a pie chart (Figure 2), using the making drawing strategy *as* a problem-solving strategy. A pie graph is a circle in which the slices represent percentages (Steinberg, 2008). This will require the use of proportions: 48 out of 100 respondents play soccer (48/100) and 52 out of 100 (52/100). These fractions need to be converted into equivalent fractions as part of the whole 360°, an operation that requires proportional reasoning. Learners are given an opportunity to work with fractions, carry out multiplication to find the portion of 360° that will represent a particular characteristic and draw the corresponding sector of the pie. To draw the pie charts, the following steps can be taken: The proportion are: $\frac{48}{100}$ and $\frac{52}{100}$. The "regle de trois" (Hersant, 2001) can be used to find the equivalent fraction of 360°. 100° corresponds to $\frac{360^{\circ} \times 52}{100}$. Thus, 48% corresponds to $\frac{360^{\circ} \times 48}{100} = 172.8^{\circ}$ and 52% correspond to $\frac{360^{\circ} \times 52}{100} = 187.2^{\circ}$.





The pie chart shows that 172.8° represents the 48% of respondents who feel that the Government has handled the lockdown and pandemic crisis very well. While, the pie chart displays 187.2°, representing 52% of respondents that believe it has not been handled well at all.

The above discussion shows that the problem solving requires a variety of skills including interpreting information, planning and methodical working, checking results, and trying alternative strategies (Muir, Beswick, & Williamson, 2008). A teachers' understanding and recognition of students' problem solving strategies used in the problem solving-Mathematics classroom, therefore, should be promoted and this can also be done in the Statistics classroom.

Cooperative Group Work

Cooperative group work can be used in both Mathematics and Statistics activities. Cooperative group work occurs when learners work in small groups to help each other learn. Researchers have found that cooperative group work can be an effective strategy for improving achievement (Santrock, 2009). According to Ben-Zvi *et al.* (2008), conducting a cooperative lesson typically involves four steps: Making pre-instructional decisions about the lesson; Explaining the task and cooperative structure to learners; Monitoring and, if necessary, intervening with each learning group after the lesson; Processing and evaluating learner achievement. In South Africa, the National Curriculum Statement aims to produce learners that are able to work effectively as individuals and with others as members of a team (DBE, 2011).

Conceptual and Procedural Knowledge

Recently, the teaching process has shifted its focus towards a balance between procedural and conceptual understanding (Zakarie, 2011). Conceptual

Mathematics understanding is knowledge that involves a thorough understanding of underlying and foundational concepts behind the algorithms performed in Mathematics (Hope, 2006). Students use conceptual undestanding of Mathematics when they identify and apply principles, know and apply facts and defintions, and compare and contrast related concepts (NCTM, 2000). Procedural Mathematics understanding is knowledge that focuses on skills and step-by-step procedures without explixit reference to mathematical ideas (Hope, 2006). Hope (2006) revealed that conceptual Mathematics understanding includes the knowledge of basic statistical facts. Moreover procedural understanding is representation of tasks which involve application of standard notation, representation and algorithms to solve statistical problems (Lipson, 2007). According to Lim (2002) procedural understanding can aid in understanding conceptual understanding. Every student should learn Mathematics with understanding (Hope, 2006). This might be the case with every student in learning Statistics. This is in alignment with the aims of South African Mathematics Curriculum. This Curriculum aims to ensure that children acquire and apply knowledge and skills in ways that are meaningful to their own lives. In this regard, the Mathematics Curriculum aims to produce learners that can collect, analyse, organise, and critically evaluate information; communicate effectively using visual, symbolic and/or language skills in various modes (DBE, 2011).

Link between Statistics and Mathematics

In South Africa, the Mathematics Curriculum consists of ten different content areas such as: Function; Number patterns, sequences, series; Finance, growth, decay; Algebra; Differential calculus; Probability; Euclidean Geometry, and Measurement; Analytical Geometry; Trigonometry; Statistics. Each content area contributes towards the acquisition of the specific skills (DBE, 2011). But these content areas are highly interconnected.

Algebra serves as one of the basic building blocks of Statistics. A natural link exists between data analysis in Statistics and algebra. Algebra is more than a set of procedures for manipulating symbols; it provides a way to explore, analyse, and represent mathematical concepts and ideas (National Council of Teachers of Mathematics, 2009). Algebra describes relationships that are purely mathematical or that arise in real-world phenomena and are modelled by algebraic expressions and presented on graphs. Learners' understanding of functions and graphs functions can both develop and be enhanced by addressing problems that involve data analysis and Statistics in authentic situations. Moreover, the representation on the Cartesian plane permits to link the properties of a function to those of a graph of that function. Cazorla, Silva and Utsumi, (2008) declared that analytic geometry can appear as a field of confluence of several concepts such as function, equation, and geometrical figure. Thus, Cazorla et al. (2008) concluded that there is a link between analytical geometry and Statistics.

Methodology

Aims of the Study

This paper sought to explore the relation between the teaching of mathematics and the teaching of statistics at high school level in the South African Context, Furthermore, this study pursued to examine and analyse examples of statistical teaching situations from both a mathematical and a statistical perspective with view to reveal the links between the teaching of mathematics and teaching of statistics.

Research Design

This study adopted a qualitative approach. A non-empirical method was followed to achieve the aims of the study. A literature review was used to answer to the critical aspects of the study.

Results

A review of the relation between the teaching of Mathematics and the teaching of Statistics in the South African context could play a role in the teaching of Statistics at high school. Based on the aims of the study literature review revealed that the South African views of Mathematics are closely associated with those of the progressive educators and the social reformers. Furthermore, literature review identified three desired learning outcomes in the teaching of Statistics, namely statistical literacy, statistical reasoning, and statistical thinking. This implies that teachers need: to develop learners' skills such: collect, analyse, and organise quantitative data to evaluate and critique conclusions; Communicate appropriately by using descriptions in words, graphs, symbols, tables, and diagrams. Teachers need to foster active learning by way of various alternatives approaches to teaching. Additionally, the literature review revealed that there is indeed a relation between the teaching of Statistics and the teaching of Mathematics based on the influence of constructivism, existing knowledge, problem-solving, cooperative learning, and the conceptual and procedural knowledge. Acknowledging the links between the teaching of Mathematics and the teaching of Statistics will enhance the instruction that teachers provide to their learners and promote an awareness of the ways in which Statistics is presented at high school.

Discussion

In South Africa, Statistics is part of the Mathematics Curriculum at high school, but yet Statistics differs from Mathematics. Verhoeven (2009, p. 10) revealed that the evidence that Statistics differs from Mathematics is not

presented to argue that Mathematics is not important to Statistics or that Statistics should not be part of Mathematics. To the contrary, mathematics conceptual understanding forms part of the basic Statistics. The South African Mathematics Curriculum supports a learner-centred teaching approach whereby the teacher is the one that exposes learners to mathematical experiences (DBE, 2011). This is also the case for Statistics in high school, where the teachers focus on the statistical concepts and later on the method. Thus, the teacher needs to consider the Mathematics concepts involved in Statistics and discuss these with the class. This can still be done in class and bearing in mind about learners' Mathematics prior

In the teaching of statistics, learners' statistical literacy, statistical reasoning and statistical thinking should be developed. These strictly depend on context. Verhoeven (2009, p. 10) confirms that this means that Mathematics serves Statistics only when it is absolutely necessary to understand statistical concepts.

Conclusions

This study explored the relation between the teaching of Mathematics and the teaching of Statistics at high school level in the South African Context. Furthermore, the study examined and analysed examples of statistical teaching situations from both a mathematical and a statistical perspective with view to reveal the links between the teaching of Mathematics and teaching of Statistics. In this study, a literature review on the teaching of Mathematics and Statistics were conducted.

The findings seem to indicate that there is indeed a relation between the teaching of Statistics and the teaching of Mathematics based on the influence of constructivism, existing knowledge, problem-solving, cooperative learning, and the conceptual and procedural knowledge. The teaching Statistics could be improved if the Mathematics teachers should get to know and understand the links between the teaching of Mathematics and the teaching of Statistics in order to be able to teach Statistics more effectively. The envisaged improvement will enhance the teaching of Statistics at high school.

Therefore, Statistics must be presented in a manner that seeks to acknowledge the changes resulting from the Curriculum transformation in South Africa as well as from the developments in Statistics research abroad.

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