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COM2014-0943

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An Introduction to
ATINER's Conference Paper Series

This paper should be cited as follows:

Bedalli E. and Ninka I., (2014) **"Exploring an Educational System's Data through Fuzzy Cluster Analysis",** Athens: ATINER'S Conference Paper Series, No: **COM2014-0943.**

Exploring an Educational System's Data through Fuzzy Cluster Analysis

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Abstract

Clustering is a very useful technique which helps to enrich the semantics of the data by revealing patterns in large collections of poly-dimensional data. Moreover the fuzzy approach in clustering provides flexibility and enhanced modeling capability, as the results are expressed in soft clusters, allowing partial memberships of data points in the clusters.

During the last decade, the digitalization of detailed student records of the University of Elbasan has not only simplified the typical university procedures but also it has created the possibility of a deeper view of the students' data. The cluster analysis applied on these student data can discover patterns which would assist in several strategic issues like: optimizing the student advising process, organization of curricula, adjusting the compulsory/elective courses, preparing better teaching approaches etc.

In our study, besides the classical fuzzy c-means, we will utilize several other variations like the possibilistic fuzzy c-means, the Gustafson-Kessel algorithm and the kernel based fuzzy clustering. We have found the application of several variations of the fuzzy clustering algorithms on these data to be a productive approach. Particular applications sometimes provide useful viewpoints which trigger innovative ideas for the policy-makers of the university.

Key Words: fuzzy cluster analysis, fuzzy c-means, possibilistic c-means, kernel based clustering, performance analysis

Introduction

Clustering algorithms are important instruments used in the analysis of large collections of data. They are typically unsupervised methods which arrange the data elements into classes (clusters) based on the similarity among the data elements, thus revealing underlying patterns of the data (Hoppner et al., 1999). Due to its fair modeling capabilities even without prior knowledge about the distribution of the data, cluster analysis has a wide range of applicability in various disciplines of study like patterns recognition, image processing, cognitive sciences, economics, medicine, education etc (Miyamoto et al., 2008)

The fuzzy approach to cluster analysis generalizes the concept of the distribution of the data elements into clusters relaxing the condition that each data element must belong to exactly one of the clusters, thus allowing each data element to have partial membership (a value between 0 and 1) into several clusters simultaneously. This is of particular interest in the cases when the boundaries among the classes (clusters) are not clearly separated (they are blurred). Furthermore the resulting partial memberships may be helpful in revealing more sophisticated relationships between the data elements and the created clusters (Hoppner et al., 1999). The most widely-used fuzzy clustering algorithm is the fuzzy c-means algorithm (FCM). Several variations of this algorithm are developed by trying to optimize the algorithm efficiency on specific scenarios and by analyzing the influence of various parameters characterizing the algorithm like the fuzzy exponent, the distance measure etc. Some of the most-important variations of the FCM algorithm include but are not limited to Gustafson-Kessel algorithm (GK), Gath-Geva algorithm (GG), possibilistic fuzzy clustering algorithm (PFCM), kernel-based fuzzy clustering algorithm (KFCM) etc.

In this paper we have conducted an experimental study by applying several fuzzy cluster analysis techniques to explore the collection of student's data available in the Information Systems Center at the University of Elbasan. We have applied several algorithms on these data and we have described the interpretations and utilization of the obtained outcomes in the improvement of some aspects of the education process. Moreover we have outlined perspectives of further applications. The main application was in the improvement of the student advising process. This was achieved by profiling the students according to their data and providing guidance to improve their academic performance. Also the student advising process was assisted in the suggestion of the selection of the elective courses according to the characterizations obtained by the fuzzy cluster analysis. Outcomes of the analysis were also interpreted to the lecturers for to assist them in development of better teaching approaches.

Fuzzy Cluster Analysis

The fuzzy clustering algorithms are classified into two major categories: the partitional clustering algorithms and hierarchical clustering algorithms. The algorithms in the partitional category generate a single partition of the data set, while the hierarchical clustering algorithms generate a nested sequence of partitions (Miyamoto et al., 2008). In this paper we will be focused only on partitional clustering algorithms. In the following subsections we will discuss respectively the fuzzy c-means algorithm, the Gustafson-Kessel algorithms, the possibilistic fuzzy c-means algorithm and the kernel-based fuzzy c-means algorithm. Finally we will briefly describe the crucial problem determining of the optimal number of clusters, known as the cluster validity problem.

Fuzzy C-Means Clustering

This algorithm operates in a data set in an unsupervised way aiming to categorize the data elements into several clusters (classes) based on some distance metric which estimates the dissimilarity between the data points. Thus the algorithm tends to partition the data elements into several clusters where the elements in the same cluster are closer (shorter distance) to each other than to the elements in the other clusters. The elements may have partial membership in several clusters, while the sum of the membership values into distinct clusters must be equal to 1. The algorithm tries to minimize the objective function: $J = \sum_{i=1}^{n} \sum_{j=1}^{c} \mu_{ij}^{\varphi} \, d^2(x_i, c_j)$ where n represents the number of elements in the data set, c represents the number of the clusters, c_j the center (prototype) of the j-th cluster, x_i the i-th element, μ_{ij} the membership of the x_i element in the c_j cluster, $d^2(x_i, c_j)$ the square of the distance from x_i to c_j according to some distance metrics (dissimilarity metrics), and φ the fuzzy exponent which varies in $[1, \infty)$. There are several possible choices for the distance metrics like the Euclidean distance, the Manhattan distance, the Minkowski distance, the maximum distance, the Pearson correlation distance etc.

The algorithm takes as input the number of the clusters (c), the fuzzy exponent φ (such that φ > 1) and the tolerance scale ε. The algorithm is described by the given pseudo-code (Hoppner et al., 1999):

1. Pick c (random) points as the initial centers of the clusters.
2. Assign k=1
3. Compute the distance from each point and each center according to chosen distance metrics.

4. Update the partition matrix $U_k = [\mu_{ij}]$, with entries $\mu_{ij} = \dfrac{d_{ij}^{-\frac{2}{\varphi-1}}}{\sum_{k=1}^{c} d_{ik}^{-\frac{2}{\varphi-1}}}$

5. Compute the new centers $c_i = \dfrac{\sum_{j=1}^{n} \mu_{ij}^{\varphi} x_j}{\sum_{j=1}^{n} \mu_{ij}^{\varphi}}$

6. If $\|U_k - U_{k-1}\| < \varepsilon$ then TERMINATE, otherwise increment k and jump to step 3.

The Gustafson-Kessel Algorithm

This algorithm is an extension of the FCM algorithm which modifies the distance metric which is used. In this case an adaptive distance metric is used. The objective function of the GK algorithm is the same as in the FCM, while the distance metric becomes (Liu et al., 2008):

$$d^2(x_i, c_j) = \|x_i - c_j\|^2 = (x_i - c_j)^T V_i (x_i - c_j)$$

where $V_i = |\Sigma_i|^{1/p} \Sigma_i^{-1}$, and $\Sigma_i = \dfrac{\sum_{i=1}^{c} \sum_{j=1}^{n} \mu_{ij}^{\varphi} (x_i - c_j)^T (x_i - c_j)}{\sum_{i=1}^{c} \sum_{j=1}^{n} \mu_{ij}^{\varphi}}$

The algorithm is described by the given pseudo-code (Liu et al., 2008):
1. Pick c (random) points as the initial centers of the clusters.
2. Assign k=1.

3. Evaluate the covariance matrix: $\Sigma_i = \dfrac{\sum_{i=1}^{c} \sum_{j=1}^{n} \mu_{ij}^{\varphi} (x_i - c_j)(x_i - c_j)^T}{\sum_{i=1}^{c} \sum_{j=1}^{n} \mu_{ij}^{\varphi}}$

4. Evaluate the distance from each data element to each cluster prototype:

$$d^2(x_i, c_j) = (x_i - c_j)^T V_i (x_i - c_j) \text{, where } V_i = |\Sigma_i|^{1/p} \Sigma_i^{-1}$$

5. Update the partition matrix $U_k = [\mu_{ij}]$, according to:

$$\mu_{ij} = \left[\sum_{k=1}^{c} \left(\frac{d(x_j, c_i)}{d(x_j, c_k)} \right)^{2/(\varphi - 1)} \right]^{-1}$$

6. Evaluate the new prototypes $c_i = \dfrac{\sum_{j=1}^{n} \mu_{ij}^{\varphi} x_j}{\sum_{j=1}^{n} \mu_{ij}^{\varphi}}$

7. If $\|U_k - U_{k-1}\| < \varepsilon$ then TERMINATE, otherwise increment k and continue to step number 3.

Possibilistic Fuzzy C-Means Clustering

The possibilistic fuzzy c-means clustering technique was developed in 1997 by Pal and Bezdek, when they suggested an improvement to the possibilistic c-means clustering algorithm by taking into consideration both the typicality values of the possibilistic version and the fuzzy values of the fuzzy version of the c-means algorithm (Pal et al., 2008). The objective function of this algorithm is:

$$J = \sum_{i=1}^{c} \sum_{j=1}^{n} (a \mu_{ij}^{\varphi} + b t_{ij}^{\rho}) \times d^2(x_i, c_j) + \sum_{i=1}^{c} \delta_i \sum_{j=1}^{n} (1 - t_{ij})^{\rho}$$

The constraints are $\sum_{i=1}^{c} \mu_{ij} = 1 \ \forall j, 0 \le \mu_{ij}, t_{ij} \le 1$ and $\varphi, \rho > 0$. The coefficients a and b are positive real numbers which represent the relative

significance of the membership values and the typicality values (Pal et al., 2008;

The membership values are evaluated by: $\mu_{ij}=\dfrac{d_{ij}^{-\frac{2}{\varphi-1}}}{\sum_{k=1}^{c}d_{ik}^{-\frac{2}{\varphi-1}}}$, the typicality

values are evaluated by $t_{ik}=\dfrac{1}{1+\dfrac{b\,d^2(x_i,c_j)}{\delta_i}}$ and new centers

$c_i=\dfrac{\sum_{j=1}^{n}\left(a\,\mu_{ij}^{\varphi}+b\,t_{ij}^{\rho}\right)x_j}{\sum_{j=1}^{n}\left(a\,\mu_{ij}^{\varphi}+b\,t_{ij}^{\rho}\right)}.$

As it may be noticed the requirement that the typicality values at any certain cluster must sum up to one is cancelled, as it complicates the situation especially for large data sets (Ojeda-Magafia et al, 2006).

The Kernel-based Fuzzy C-Means Clustering
The kernel-based fuzzy c-means clustering technique is a modification of the conventional fuzzy c-means clustering technique by employing a nonlinear map (known as the kernel function) from the feature space to a high dimensional kernel space. This nonlinear map enables the identification of complex structures (which cannot be linearly separated in the feature space), as in the kernel space they are transformed into simpler linearly separable structures (Zhang & Chen, 2003). The nonlinear map is denoted as: $\Phi: x \rightarrow \Phi(x)$. The objective function that we tend to minimize is:

$$J = \sum_{i=1}^{n}\sum_{j=1}^{c} \mu_{ij}^{\varphi} \left\| \Phi(x_i) - \Phi(c_j) \right\|^2$$

Here we have $\left\| \Phi(x_i) - \Phi(c_j) \right\|^2 = K(x_i,x_i) + K(c_j,c_j) - 2K(x_i,c_j)$ where $K(x,y)$ is an inner product kernel (Zhang & Chen, 2003; Graves & Pedrycz, 2010). In our study we have employed the Gaussian function as kernel function, i.e. $K(x_i,x_j) = e^{-\frac{\left\|x_i-x_j\right\|^2}{2\sigma^2}}$ where $\sigma \in R$, so $K(x,x) = 1$ and the objective function is expressed as:

$$J = 2 \sum_{i=1}^{n}\sum_{j=1}^{c} \mu_{ij}^{\varphi} \left(1 - K(x_i,c_j)\right)$$

The algorithm is described by the given pseudo-code :
1. Pick c (random) points as the initial centers of the clusters.
2. Assign k=1.

3. Evaluate the new prototypes $c_i = \dfrac{\sum_{j=1}^{n} \mu_{ij}^{\varphi} K(x_j,c_i) x_j}{\sum_{j=1}^{n} \mu_{ij}^{\varphi} K(x_j,c_i)}$

4. Update the partition matrix $U_k = [\mu_{ij}]$, by

$\mu_{ij}=\dfrac{(1/(1-K(x_j,c_i)))^{1/(m-1)}}{\sum_{k=1}^{c}(1/(1-K(x_j,c_k)))^{1/(m-1)}}$

5. If $\|U_k - U_{k-1}\| < \varepsilon$ then TERMINATE, otherwise increment k and continue to step number 3.

The Cluster Validity Problem

One of the critical problems associated with the clustering algorithms is to answer the question whether the obtained clusters are optimal, which is known as the cluster validity problem. As the clustering algorithms are unsupervised, we have no prior labels to assess the classification accuracy. Under these circumstances the quality of the resulting clusters is assessed based on their compactness and separation. Compactness is a quantity that evaluates the variation of the data within the same cluster separation is a quantity that describes the structures among the different clusters. The primary goal of all the validation methods is to decrease the compactness and to increase the separation of the obtained clusters. There are several well-known cluster validation techniques like the partition coefficient, the partition index, the partition entropy, the partition index, the separation index, the Xie-Beni index, the Fukuyama-Sugeno index, the fuzzy hypervolume etc (Bedalli & Ninka, 2013). In this paper we will utilize three of these validity measures: the partition index, the Xie-Beni index and the fuzzy hypervolumes. The partition index estimates the amount of shared regions among the clusters. It is calculated as:

$$PC(c) = \frac{1}{N} \sum_{i=1}^{c} \sum_{j=1}^{N} (\mu_{i,j})^2$$

with $\mu_{i,j}$ representing the membership value of the $j-th$ data element in the $i-th$ cluster. The value satisfies the inequality $\frac{1}{c} \leq PC(c) \leq 1$. The drawback of this method is that it monotonically decreases with c and there is no explicit relation to some property of the data. The optimal value of c is the value that maximizes the partition coefficient.

The Xie-Beni index is evaluated as:

$$XB(c) = \frac{\sum_{i=1}^{c} \sum_{j=1}^{N} (\mu_{i,j})^m \|x_j - v_i\|^2}{N \min_{i,j} \|x_j - v_i\|^2}$$

with $\mu_{i,j}$ representing the membership value of the $j-th$ data element in the $i-th$ cluster, x_j is the $j-th$ data element, and v_i is the center of the i-th cluster. The optimal value of c is the value that minimizes the index (Bedalli & Ninka, 2013).

The fuzzy hypervolumes is one of the most frequently used validity measures. It can be considered as the volume of the fuzzy clusters and it is calculated as:

$$\Upsilon(c) = \sum_{i=1}^{c} \det(F_i)$$

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So it is expressed as the sum of the determinant of the F_i matrices, where F_i represents the matrix:

$$F_i = \frac{\sum_{j=1}^{N} \mu_{ij}^m (x_j - v_i)(x_j - v_i)^T}{\sum_{j=1}^{N} \mu_{ij}^m}$$

Methodology and Interpretation of Results

The fuzzy clustering techniques which were theoretically discussed in the previous sections of this paper have been applied to explore the collection of student's data available in the Information Systems Center at the University of Elbasan. One of the troublesome aspects of the fuzzy c-means algorithm and its variations is the large computational complexity especially when the data elements have many dimensions. Clustering in the multi-dimensional feature spaces is a challenging task not only because it is a time intensive process, but also the presence of outliers and noisy data would affect the results in a more sensitive manner (Eschrich et al., 2003; Hogo 2010). In our case the data elements consist of many features which may be discrete, continuous or categorical. Involving all these features simultaneously would yield implementation challenges and computational infeasibilities. So our first step in our approach (considered as a preprocessing stage) was to reduce the dimensionality of the data elements. The reduction was achieved through three main strategies which were feature selection, quantization and aggregation.

Through feature selection only the most representative features of the data elements are picked in order to be involved in the evaluation of the similarity (or dissimilarity) between the data elements. On the other hand, through quantization continuous data of various types are transformed and adapted in the discrete form. There are cases of precision loss when using quantization, but generally they yield insignificant changes in the results (Eschrich et al., 2003). Finally through aggregation we combine and merge several features into a single weighted feature. The value of this new feature will be the representative value which will be involved in the evaluation of the similarity (or dissimilarity) between the data elements (Eschrich et al., 2003; Talavera & Gaudioso, 2004).

After we have reduced the dimensionality of the data elements in our collection, then we have applied several times the clustering algorithms like the fuzzy c-means clustering, the Gustafson-Kessel clustering algorithm, the fuzzy possibilistic clustering and the kernel-based fuzzy c-means clustering. The algorithms were applied with the value 2 for the fuzzy exponent, the value 0.0001 for the scale of tolerance and several values for the number of clusters varying iteratively from 2 to 10. Later we have validated the obtained clusters through three cluster validation techniques, namely the partition index, the Xie-Beni index and the fuzzy hyper volumes measure. Through the validation process we have determined the optimal number of clusters for each case and the membership values of the optimal partition. The obtained partitions are

utilized in the next subsections to address important aspects of the education process as the student advising, the recommendations about the elective courses and the adaption of better teaching approaches.

Assisting the Student Advisors

Typically an advisor, who is in the same time a lecturer/teaching assistant, is assigned to each class in our university. The advisor's main duties generally consists of the students orientation about the offered courses in each semester, about the regulations in various aspects of the university procedures, about the utilization of various resources of the university and to consult the students about difficulties/poor performances they may be facing. The student advising process is generally difficult to be handled in a customized way (Romero & Ventura, 2010). The advisors typically give advices based on the grade point average of the student and the information about grade distribution of various courses in the previous years. This approach cannot provide specific guidance to the students, as it is difficult to characterize their profiles based just on their grade point average and the grade distribution in various courses.

Our application aims to provide more useful information to the advisors about the students' profiles by summarizing to them the fuzzy cluster analysis outcomes. We have applied several clustering techniques and through cluster validation measures we have selected the optimal partition. Cluster validation is very useful as it primarily determines the optimal number of clusters. These clusters will be the main categories to characterize the student profiles. Based on the number of the clusters and on the values of the cluster centers (prototypes) these clusters are manually labeled.

As an illustrating example we are describing the outcomes of the fuzzy cluster analysis about the first three semesters for the students registered in the Information Technologies program of study in the year 2011-2012. After the clustering algorithms were applied several times with varying number of initial clusters (we have iterated the clustering procedures with values of c from 2 to 10), the cluster validation procedures evaluated the optimal partition to contain 5 clusters and the most appropriate membership values were those generated by the kernel–based fuzzy clustering technique. These clusters were labeled as "Very good", "Good", "Average", "Sufficient" and "Insufficient". For each student the partial memberships into these clusters (categories) are provided. Table 1 summarizes a few entries containing the membership values of some students in the respective categories.

Table 1. *The Membership Values of a Few Students in the Generated Clusters*

Student No.	Very Good	Good	Average	Sufficient	Insufficient
1	0.0106	0.0512	0.8681	0.0610	0.0091
2	0.0326	0.6348	0.2075	0.0784	0.0467
3	0.0012	0.0074	0.0368	0.0521	0.9025
4	0.7645	0.1204	0.0654	0.0349	0.0148
5	0.0085	0.0161	0.0912	0.5718	0.3124
6	0.0215	0.2140	0.6123	0.1352	0.0170
7	0.0124	0.0732	0.7921	0.1139	0.0084
8	0.2735	0.5518	0.1276	0.042	0.0051
9	0.0103	0.1083	0.5914	0.2715	0.0185
10	0.0028	0.0306	0.0816	0.3538	0.5312
11	0.0109	0.0243	0.2154	0.6210	0.1284
12	0.1931	0.6704	0.0822	0.0475	0.0068
13	0.7105	0.2462	0.0434	0.0123	0.0076
14	0.0037	0.0105	0.0320	0.1432	0.8106
15	0.0073	0.03165	0.9135	0.04215	0.0054

The fuzzy clustering results provide more information for the advisor then the hard clustering would provide. For example both the fifth and eleventh student in the given table in the case of hard clustering would belong completely to the "Sufficient" category, without any further information being provided. In our case, certainly these students both have the largest value of their memberships in the "Sufficient" category but for the fifth student the advisor would advise him to take care not to fall in the insufficient category, while the eleventh student would be prompted to achieve the "Average" category. Similarly the second and the twelfth student would both be classified in the "Good" category, but the second one is in the lower part of this category and the twelfth one is in the upper part of this category.

Elective Courses Recommendations

Choosing a course from a group of elective courses is generally a procedure in which the students would require recommendation. In our approach we aimed to give recommendations to the students based on their profile characterization about the previous courses which are considered related to the courses to be elected. More concretely in our illustrating example we try to give recommendations to guide the students to choose among two elective courses, namely "Distributed systems" and "Parallel computing". For the "Distributed systems" course we have used aggregation of the data of three previous courses: "Computer Architecture", "Operating systems" and "Computer Networks", and for the "Parallel computing" course we have used aggregation of the data about three previous courses: "Introduction to

programming", "Discrete mathematics" and "Analysis of algorithms". After the aggregation step (considered as e preprocessing stage) we have applied the fuzzy cluster analysis techniques. The fuzzy clustering techniques were applied iteratively with values of c (number of clusters) varying from 2 to 8. Finally the cluster validation techniques were applied to select the optimal partitions. In this case the optimal number of partitions was 4, and the most appropriate membership values were generated by the Gustafson-Kessel clustering algorithm. The resulting four clusters were labeled as "High", "Satisfactory", "Sufficient" and "Insufficient".

In table 2 are shown some results about the memberships of a few students in the clusters for the "Distributed systems" course (which is generated by the aggregation of the data of three previous courses: "Computer Architecture", "Operating systems" and "Computer Networks").

Table 2. *The Membership Values of a Few Students for the "Distributed Systems" Course Recommendation*

Student No.	High	Satisfactory	Sufficient	Insufficient
1	0.3106	0.5712	0.1053	0.0129
2	0.0609	0.1639	0.6427	0.1325
3	0.8204	0.1275	0.0473	0.0048
4	0.0451	0.9210	0.0211	0.0128
5	0.0247	0.1055	0.7742	0.0956

In the table 3 are shown the results about the memberships of the same few students in the clusters for the "Parallel programming" course (which is generated by the aggregation of the data of the three previous courses: "Introduction to programming", "Discrete mathematics" and "Analysis of algorithms").

The (complete versions of these) tables are provided to the advisors to guide them for giving recommendations to the students whether to select the "Distributed systems" or the "Parallel computing" elective courses.

Table 3. *The Membership Values of a Few Students for the "Parallel Programming" Course Recommendation*

Student No.	High	Satisfactory	Sufficient	Insufficient
1	0.0496	0.1922	0.6357	0.1225
2	0.7193	0.2154	0.0586	0.0067
3	0.8926	0.0685	0.0373	0.0016
4	0.2320	0.6512	0.0854	0.0314
5	0.0865	0.8012	0.0954	0.0169

According to the evaluated membership values, the first student would be recommended to choose the "Distributed systems" course, the second and fifth students would be advised to choose the "Parallel programming" course. As for the third and fourth student, an advisor would not prefer to recommend primarily any of the two courses, but would leave the choice completely on the student's preferences.

We are planning as a future research to study the results of the students who have required recommendation and to compare them statistically to the results of the students in the previous years. Also we are planning to extend these studies to develop recommender systems in an automated way for other elective courses.

Assisting the Lecturers for Better Teaching Approaches

Another form of utilization of the results generated by the fuzzy cluster analysis was to provide them to lecturers for better teaching approaches (Talavera & Gaudioso, 2004). More concretely after the cluster analysis is completed and the cluster validation measures have been applied to determine the optimal partitions which characterize the students' performances, these results are utilized by the lecturers to adjust the assignments and the course projects. As it is known assignments and course projects are frequently used in the evaluation of the students. Knowing the distribution of the students in the fuzzy clusters is very valuable information for the lecturers/teaching assistants while they are formulating the assignments and course projects of various courses.

Conclusions

In this paper we have discussed methods of using fuzzy cluster analysis in the exploration of the students' data in an educational information system and to use the results to improve some critical procedures of a university like the student advising, recommendations about the elective courses and prepare better teaching approaches.

Firstly we made a theoretical discussion about some of the most widely-used fuzzy clustering techniques like the fuzzy c-means algorithm, the Gustafson-Kessel algorithm, possibilistic fuzzy clustering and kernel-based fuzzy clustering algorithm. Also we discussed the critical problem of cluster validation which enables the estimation of the quality of the generated clusters.

We observed that the fuzzy clustering results provide flexibility in the characterization of the student profiles, which is very useful in the student advising process.

Another useful application of the cluster analysis was to develop recommendations for the student for their choices about the elective course. We have clustered the students based on their previous performances on the related courses.

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